

Observations of Math Lab Manual Activities for Class 11

1. To represent set theoretic operations using Venn diagrams.

Observations:

1. Coloured portion in Fig. 3.1, represents $A \cup B$ _____.
2. Coloured portion in Fig. 3.2, represents $A \cap B$ _____.
3. Coloured portion in Fig. 3.3, represents A' _____.
4. Coloured portion in Fig. 3.4, represents B' _____.
5. Coloured portion in Fig. 3.5, represents $(A \cap B)'$ _____.
6. Coloured portion in Fig. 3.6, represents $(A \cup B)'$ _____.
7. Coloured portion in Fig. 3.7, represents $B - A$ _____.
8. Coloured portion in Fig. 3.8, represents $A' \cup B$ _____.
9. Fig. 3.9, shows that $(A \cap B) = \phi$ _____.
10. Fig. 3.10, represents $A \subset B$.

2. To find the values of sine and cosine functions in second, third and fourth quadrants using given values in the first quadrant.

Observations:

1. Angle made by the needle in one complete revolution is 2π OR 360° _____.
2. $\cos \frac{\pi}{6} = \frac{\sqrt{3}}{2} = \cos \left(-\frac{\pi}{6}\right)$
 $\sin \frac{\pi}{6} = \frac{1}{2} = \sin(2\pi + \frac{\pi}{6})$.
3. sine function is non-negative in First and Second quadrants.
4. cosine function is non-negative in First and Fourth quadrants.

3. To prepare a model to illustrate the values of sine function and cosine function for different angles which are multiples of $\frac{\pi}{2}$ & π .

Observations:

1. When radius line of circular plate is at 0° indicating the point A (1,0),

$$\cos 0 = \underline{\underline{1}} \text{ and } \sin 0 = \underline{\underline{0}}.$$

2. When radius line of circular plate is at 90° indicating the point B (0, 1),

$$\cos \frac{\pi}{2} = \underline{\underline{0}} \text{ and } \sin \frac{\pi}{2} = \underline{\underline{1}}.$$

3. When radius line of circular plate is at 180° indicating the point C (-1,0),

$$\cos \pi = \underline{\underline{-1}} \text{ and } \sin \pi = \underline{\underline{0}}.$$

4. When radius line of circular plate is at 270° indicating the point D (0, -1)

$$\text{which means } \cos \frac{3\pi}{2} = \underline{\underline{0}} \text{ and } \sin \frac{3\pi}{2} = \underline{\underline{-1}}.$$

5. When radius line of circular plate is at 360° indicating the point again at A

$$(1,0), \cos 2\pi = \underline{\underline{1}} \text{ and } \sin 2\pi = \underline{\underline{0}}.$$

Now fill in the table :

Trigonometric Function	0	$\frac{\pi}{2}$	π	$\frac{3\pi}{2}$	2π	$\frac{5\pi}{2}$	3π	$\frac{7\pi}{2}$	4π
$\sin \theta$	0	1	0	-1	0	1	0	-1	0
$\cos \theta$	1	0	-1	0	1	0	-1	0	1

4. To interpret geometrically the meaning of $i = \sqrt{-1}$ and its integral powers.

Observations:

1. On rotating OA through 90° , $OA_1 = 1 \times i = \underline{\underline{i}}$.

2. On rotating OA through an angle of 180° , $OA_2 = 1 \times i \times i = i^2 = -1$.

3. On rotation of OA through 270° (3 right angles), $OA_3 = 1 \times i \times i \times i = i^3 = -i$.

4. On rotating OA through 360° (4 right angles), $OA_4 = 1 \times i \times i \times i \times i = i^4 = 1$.

5. On rotating OA through n -right angles $OA_n = 1 \times i \times i \times i \times i \times \dots \times i \times \dots n \text{ times} = i^n$.

5. To distinguish between a Relation and a Function.

Observations:

1. In Fig. 6.3, ordered pairs are $(a, 1), (a, 2), (b, 1), (b, 2), (c, 2)$.

These ordered pairs constitute a **Relation** but not a **Function** .

2. In Fig. 6.4, ordered pairs are $(a, 1), (b, 1), (c, 1)$. These constitute a **Relation** as well as **Function** .

3. In Fig 6.5, ordered pairs are $(a, 2), (b, 2), (c, 2)$. These ordered pairs constitute a **Relation** as well as **Function** .

4. In Fig. 6.6, ordered pairs are $(b, 1), (c, 2)$. These ordered pairs do not represent **Function** but represent **Relation** .

6. To plot the graphs of $\sin x$, $\sin 2x$, $2\sin x$ and $\sin\frac{x}{2}$, using the same coordinate axes.

Observations:

1. Graphs of $\sin x$ and $2\sin x$ are of same shape but the maximum height of the graph of $\sin x$ is **half** the maximum height of the graph of **$2\sin x$** .

2. The maximum height of the graph of $\sin 2x$ is **1** . It is at $x = \frac{\pi}{4}$.

3. The maximum height of the graph of $2\sin x$ is **2** . It is at $x = \frac{\pi}{2}$.

4. The maximum height of the graph of $\sin\frac{x}{2}$ is **1** . It is at $\frac{x}{2} = \frac{\pi}{2}$.

5. At $x = \underline{0}$ and π , $\sin x = 0$, at $x = \underline{0, \frac{\pi}{2}}$ and π , $\sin 2x = 0$ and at $x = \underline{0}$ and 2π , $\sin\frac{x}{2} = 0$.

6. In the interval $[0, \pi]$, graphs of $\sin x$, $2\sin x$ and $\sin\frac{x}{2}$ are **above** x-axes and some portion of the graph of $\sin 2x$ lies **below** x-axes.

7. Graphs of $\sin x$ and $\sin 2x$ intersect at $x = \frac{\pi}{3}$ in the interval $(0, \pi)$.

8. Graphs of $\sin x$ and $\sin\frac{x}{2}$ intersect at $x = \frac{2\pi}{3}$ in the interval $(0, \pi)$.

7. To construct a Pascal's Triangle and to write binomial expansion for a given positive integral exponent.

Observations:

1. Numbers in the fifth row are 1,4,6,4,1, which are coefficients of the binomial expansion of Pascal's Triangle.
2. Numbers in the seventh row are 1,6,15,20,15,6,1, which are coefficients of the binomial expansion of Pascal's Triangle.
3. $(a + b)^3 = 1a^3 + 3a^2b + 3ab^2 + 1b^3$
4. $(a + b)^5 = a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5$.
5. $(a + b)^6 = 1a^6 + 6a^5b + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6ab^5 + 1b^6$.
6. $(a + b)^8 = a^8 + 8a^7b + 28a^6b^2 + 56a^5b^3 + 70a^4b^4 + 56b^3b^5 + 28a^2b^6 + 8ab^7 + b^8$.
7. $(a + b)^{10} = a^{10} + 10a^9b + 45a^8b^2 + 120a^7b^3 + 210a^6b^4 + 252b^5 + 210a^4b^6 + 120a^3b^7 + 45a^2b^8 + 10ab^9 + b^{10}$.

8. To construct different types of conic sections.

Observations:

1. In Fig. 21.2, the transparent plane sheet is parallel to the base of the cone. The section obtained is Circle.
2. In Fig. 21.3, the plane sheet is inclined to axis of cone. The conic section obtained is ellipse.
3. In Fig. 21.4, the plane sheet is parallel to the generator of cone. The conic section so obtained is parabola.
4. In Fig. 21.5, the plane sheet is parallel to the axis. The conic section so obtained is a part of a hyperbola.

9. Verification of the geometrical significance of the derivative.

Observations:

1. For the curve $x^2 + y^2 = 25$, $\frac{dy}{dx}$ at the point $(3, 4) = \underline{\underline{-\frac{3}{4}}}$. Value of $\theta = \underline{\tan^{-1}(-\frac{3}{4})}$, $\tan \theta = \underline{\underline{-\frac{3}{4}}}$
 $\frac{dy}{dx}$ at $(3, 4) = \underline{\underline{-\frac{3}{4}}}$.

2. For the curve $x^2 + y^2 = 25$, $\frac{dy}{dx}$ at the point $(-4, 3) = \underline{\underline{\frac{4}{3}}}$, $\tan \alpha = \underline{\underline{\frac{4}{3}}}$, $\frac{dy}{dx}$ at $(-4, 3) = \underline{\underline{\frac{4}{3}}}$.

3. For the curve $(x - 3)^2 + y^2 = 25$, $\frac{dy}{dx}$ at the point $(6, 4) = \underline{\underline{-\frac{4}{3}}}$, Value of $\theta = \underline{\tan^{-1}(-\frac{4}{3})}$, $\tan \theta = \underline{\underline{-\frac{4}{3}}}$, $\frac{dy}{dx}$ at $(6, 4) = \underline{\underline{-\frac{4}{3}}}$.

4. For the curve $xy = 4$, $\frac{dy}{dx}$ at $(2, 2) = \underline{\underline{-1}}$, $\theta = \underline{\tan^{-1}(-1)}$, $\tan \theta = \underline{\underline{-1}}$.

10. To write the sample space, when a coin is tossed once, two times, three times, four times.

Observations:

Number of elements in sample space, when a

1. coin is tossed once = 2.

2. coin is tossed twice = 4.

3. coin is tossed three times = 8.

4. coin is tossed four times = 16.

