

DIFFERENTIAL EQUATIONS

CM120901

1. Find order and degree of $5 \frac{d^2y}{dx^2} = \left\{ 1 + \left(\frac{dy}{dx} \right)^2 \right\}^{3/2}$.
2. Find order and degree of $y = px\sqrt{a^2p^2 + b^2}$, where $p = \frac{dy}{dx}$.
3. Show that the differential equation of which $y = 2(x^2 - 1) + ce^{-x^2}$ is a solution, is $\frac{dy}{dx} + 2xy = 4x^3$.
4. Find the general solution of the following differential equation: $xdy - (y + 2x^2)dx = 0$.
5. Solve the differential equation: $xdy - ydx = \sqrt{x^2 + y^2}dx$.
6. Solve : $\frac{dy}{dx} = \frac{1 - \cos x}{1 + \cos x}$.
7. Solve : $(1 + x^2) \frac{dy}{dx} - x = 2 \tan^{-1} x$.
8. Solve : $x\sqrt{1 - y^2}dx + y\sqrt{1 - x^2}dy = 0$.
9. Solve : $y(1 + e^{ex})dy = (y + 1)e^x dx$.
10. Solve : $(y + xy)dx + (x - xy^2)dy = 0$.
11. Solve : $\frac{dy}{dx} = 1 - x + y - xy$.
12. Solve : $\frac{dy}{dx} = \frac{x+y}{x-y}$.
13. Solve : $2xy \frac{dy}{dx} = x^2 + y^2$.
14. Solve : $x^2 \frac{dy}{dx} = x^2 - 2y^2 + xy$.
15. Solve : $xy \frac{dy}{dx} = x^2 - y^2$.
16. Solve : $(x^2 + 3xy + y^2)dx - x^2dy = 0$.
17. Solve : $\frac{dy}{dx} + \frac{4x}{x^2+1}y + \frac{1}{(x^2+1)^2} = 0$.
18. Solve : $\frac{dy}{dx} + y \cot x = x^2 \cos^2 x + 2x$.
19. Solve the differential equation $(x + 2y^2) \frac{dy}{dx} = y$, give that when $x = 2, y = 1$.
20. Solve : $(1 + x^2) \frac{dy}{dx} - 2xy = (x^2 + 2)(x^2 + 1)$.

